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 - ▶ Models (e.g., decision trees, linear functions, linear separators)

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- A way to handle overfitting (e.g., trade-off model complexity and fit-to-data, cross validation).

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 - ▶ Models (e.g., decision trees, linear functions, linear separators)
- A way to handle overfitting (e.g., trade-off model complexity and fit-to-data, cross validation).
- Search algorithm (usually local, myopic search) to find the best model that fits the data given the bias.

Learning Objectives - Reinforcement Learning

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- Explain the explore-exploit dilemma and solutions
- Explain the difference between on-policy and off-policy reinforcement learning

What should an agent do given:

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- Prior knowledge

Reinforcement Learning

What should an agent do given:

- **Prior knowledge** possible states of the world
possible actions
- **Observations**

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Like decision-theoretic planning, except

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Like decision-theoretic planning, except model of dynamics and model of reward not given.

Reinforcement Learning Examples

- Game -

Reinforcement Learning Examples

- Game - reward winning, punish losing

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- Dog -

Reinforcement Learning Examples

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- Dog - reward obedience, punish destructive behavior

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- Robot -

Reinforcement Learning Examples

- Game - reward winning, punish losing
- Dog - reward obedience, punish destructive behavior
- Robot - reward task completion, punish dangerous behavior

Experiences

- We assume there is a sequence of experiences:

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- The agent has to choose its action as a function of its history.
- At any time it must decide whether to
 - ▶ **explore** to gain more knowledge
 - ▶ **exploit** knowledge it has already discovered

Why is reinforcement learning hard?

- What actions are responsible for a reward may have occurred a long time before the reward was received.

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- What actions are responsible for a reward may have occurred a long time before the reward was received.
- The long-term effect of an action depend on what the agent will do in the future.
- The explore-exploit dilemma: at each time should the agent be greedy or inquisitive?

Reinforcement learning: main approaches

- search through a space of policies (controllers)

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- search through a space of policies (controllers)
- learn a model consisting of state transition function $P(s'|a, s)$ and reward function $R(s, a, s')$; solve this as an MDP.
- learn $Q^*(s, a)$, use this to guide action.

Recall: Asynchronous VI for MDPs, storing $Q[s, a]$

(If we knew the model:)

Initialize $Q[S, A]$ arbitrarily

Repeat forever:

- Select state s , action a
- $Q[s, a] \leftarrow \sum_{s'} P(s'|s, a) \left(R(s, a, s') + \gamma \max_{a'} Q[s', a'] \right)$

Reinforcement Learning (Deterministic case)

- flat or modular or hierarchical
- explicit states or features or individuals and relations
- static or finite stage or indefinite stage or infinite stage
- fully observable or partially observable
- deterministic or stochastic dynamics
- goals or complex preferences
- single agent or multiple agents
- knowledge is given or knowledge is learned
- perfect rationality or bounded rationality

Experiential Asynchronous Value Iteration for Deterministic RL

initialize $Q[S, A]$ arbitrarily

observe current state s

repeat forever:

 select and carry out an action a

 observe reward r and state s'

What do we know now?

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Temporal Differences

- Suppose we have a sequence of values:

$$v_1, v_2, v_3, \dots$$

and want a running estimate of the average of the first k values:

$$A_k = \frac{v_1 + \dots + v_k}{k}$$

Temporal Differences (cont)

- Suppose we know A_{k-1} and a new value v_k arrives:

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Let $\alpha_k = \frac{1}{k}$, then

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Let $\alpha_k = \frac{1}{k}$, then

$$\begin{aligned}A_k &= (1 - \alpha_k) A_{k-1} + \alpha_k v_k \\ &= A_{k-1} + \alpha_k (v_k - A_{k-1})\end{aligned}$$

“TD formula”

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$$\sum_{k=1}^{\infty} \alpha_k = \infty \text{ and } \sum_{k=1}^{\infty} \alpha_k^2 < \infty.$$

Q-learning

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$$Q[s, a] \leftarrow Q[s, a] + \alpha \left(r + \gamma \max_{a'} Q[s', a'] - Q[s, a] \right)$$

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Properties of Q-learning

- Q-learning converges to an optimal policy, no matter what the agent does, as long as it tries each action in each state enough.
- But what should the agent do?
 - ▶ exploit: when in state s ,
 - ▶ explore:

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- But what should the agent do?
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 - ▶ explore: select another action

Exploration Strategies

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where $\tau > 0$ is the *temperature*.

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- “optimism in the face of uncertainty”: initialize Q to values that encourage exploration.
- “upper confidence bounds” - take into account average + variance

Problems with Q-learning

- It does one backup between each experience.
 - ▶ Is this appropriate for a robot interacting with the real world?

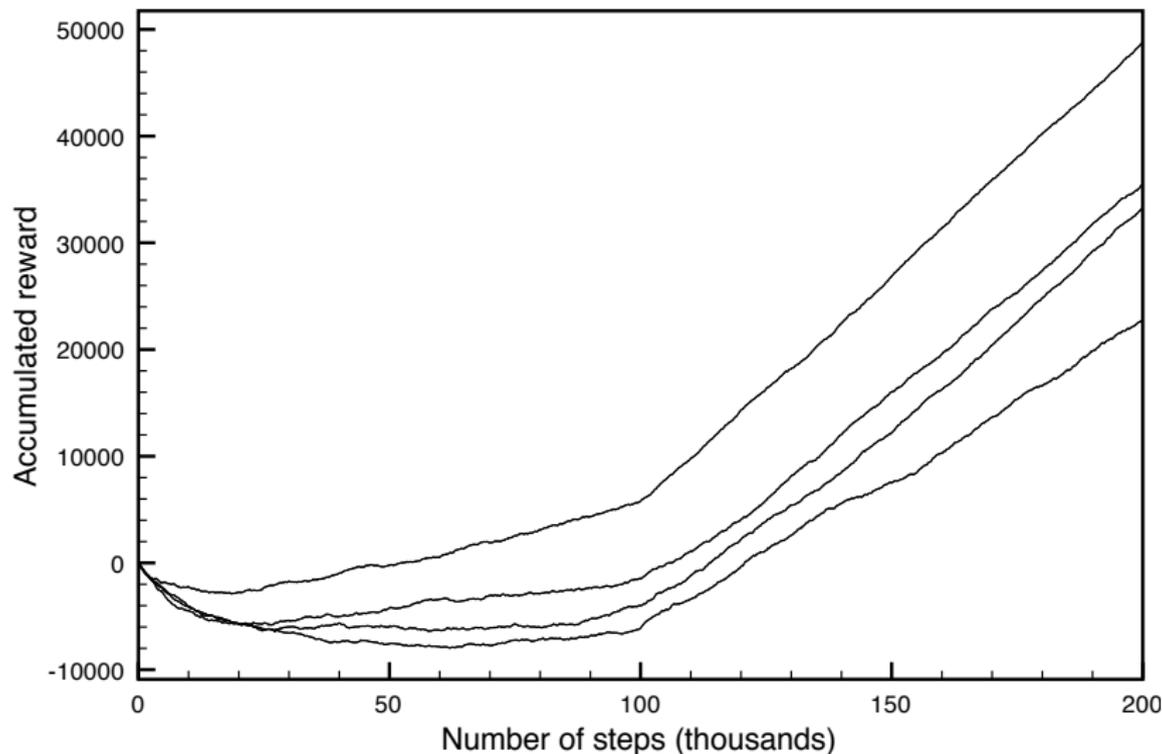
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 - ▶ Is this appropriate for a robot interacting with the real world?
 - ▶ An agent can make better use of the data by
 - doing multi-step backups
 - building a model, and using MDP methods to determine optimal policy.
- It learns separately for each state.

Evaluating Reinforcement Learning Algorithms



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- Why?

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- **On-policy learning** learns the value of the policy being followed.
e.g., act greedily 80% of the time and act randomly 20% of the time
- Why? If the agent is actually going to explore, it may be better to optimize the actual policy it is going to do.
- SARSA uses the experience $\langle s, a, r, s', a' \rangle$ to update $Q[s, a]$.

initialize $Q[S, A]$ arbitrarily

observe current state s

select action a

repeat forever:

 carry out action a

 observe reward r and state s'

 select action a' using a policy based on Q

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Reinforcement Learning with Features

- Usually we don't want to reason in terms of states, but in terms of features.
- In state-based methods, information about one state cannot be used by similar states.
- If there are too many parameters to learn, it takes too long.
- **Idea:** Express the value function as a function of the features. Most typical is a linear function of the features.

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Gradient descent

To find a (local) minimum of a real-valued function $f(x)$:

- assign an arbitrary value to x
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Linear Regression

- A linear function of variables x_1, \dots, x_n is of the form

$$f^{\bar{w}}(x_1, \dots, x_n) = w_0 + w_1x_1 + \dots + w_nx_n$$

$\bar{w} = \langle w_0, w_1, \dots, w_n \rangle$ are weights. (Let $x_0 = 1$).

- Given a set E of examples.
Example e has input $x_i = e_i$ for each i and observed value, o_e :

$$Error_E(\bar{w}) = \sum_{e \in E} (o_e - f^{\bar{w}}(e_1, \dots, e_n))^2$$

- Minimizing the error using gradient descent, each example should update w_i using:

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$$w_i \leftarrow w_i - \eta \frac{\partial Error_E(\bar{w})}{\partial w_i}$$

Gradient Descent for Linear Regression

Given E : set of examples over n features

each example e has inputs (e_1, \dots, e_n) and output o_e :

Assign weights $\bar{w} = \langle w_0, \dots, w_n \rangle$ arbitrarily

repeat:

For each example e in E :

let $\delta = o_e - f^{\bar{w}}(e_1, \dots, e_n)$

For each weight w_j :

$$w_j \leftarrow w_j + \eta \delta e_j$$

SARSA with linear function approximation

- One step backup provides the examples that can be used in a linear regression.
- Suppose F_1, \dots, F_n are the features of the state and the action.
- So $Q_w(s, a) = w_0 + w_1 F_1(s, a) + \dots + w_n F_n(s, a)$
- An experience $\langle s, a, r, s', a' \rangle$ provides the “example”:
 - ▶ old predicted value:
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- An experience $\langle s, a, r, s', a' \rangle$ provides the “example”:
 - ▶ old predicted value: $Q_{\bar{w}}(s, a)$
 - ▶ new “observed” value: $r + \gamma Q_{\bar{w}}(s', a')$

SARSA with linear function approximation

Given γ :discount factor; η :step size

Assign weights $\bar{w} = \langle w_0, \dots, w_n \rangle$ arbitrarily

observe current state s

select action a

repeat forever:

 carry out action a

 observe reward r and state s'

 select action a' (using a policy based on $Q_{\bar{w}}$)

 let $\delta = r + \gamma Q_{\bar{w}}(s', a') - Q_{\bar{w}}(s, a)$

 For $i = 0$ to n

$$w_i \leftarrow w_i + \eta \delta F_i(s, a)$$

$s \leftarrow s'$

$a \leftarrow a'$

Example Features

- $F_1(s, a) = 1$ if a goes from state s into a monster location and is 0 otherwise.
- $F_2(s, a) = 1$ if a goes into a wall, is 0 otherwise.
- $F_3(s, a) = 1$ if a goes toward a prize.
- $F_4(s, a) = 1$ if the agent is damaged in state s and action a takes it toward the repair station.
- $F_5(s, a) = 1$ if the agent is damaged and action a goes into a monster location.
- $F_6(s, a) = 1$ if the agent is damaged.
- $F_7(s, a) = 1$ if the agent is not damaged.
- $F_8(s, a) = 1$ if the agent is damaged and there is a prize in direction a .
- $F_9(s, a) = 1$ if the agent is not damaged and there is a prize in direction a .

Example Features

- $F_{10}(s, a)$ is the distance from the left wall if there is a prize at location P_0 , and is 0 otherwise.
- $F_{11}(s, a)$ has the value $4 - x$, where x is the horizontal position of state s if there is a prize at location P_0 ; otherwise is 0.
- $F_{12}(s, a)$ to $F_{29}(s, a)$ are like F_{10} and F_{11} for different combinations of the prize location and the distance from each of the four walls.

For the case where the prize is at location P_0 , the y-distance could take into account the wall.

Model-based Reinforcement Learning

- Model-based reinforcement learning uses the experiences in a more effective manner.
- It is used when collecting experiences is expensive (e.g., in a robot or an online game); an agent can do lots of computation between each experience.
- Idea: learn the MDP and interleave acting and planning.
- After each experience, update probabilities and the reward, then do some steps of asynchronous value iteration.

Model-based learner

Data Structures: $Q[S, A]$, $T[S, A, S]$, $C[S, A]$, $R[S, A]$

Assign Q , R arbitrarily, $C = 0$, $T = 0$

observe current state s

repeat forever:

select and carry out action a

observe reward r and state s'

$$T[s, a, s'] \leftarrow T[s, a, s'] + 1$$

$$C[s, a] \leftarrow C[s, a] + 1$$

$$R[s, a] \leftarrow R[s, a] + (r - R[s, a]) / C[s, a]$$

repeat for a while:

select state s_1 , action a_1

$$Q[s_1, a_1] \leftarrow R[s_1, a_1] + \sum_{s_2} \frac{T[s_1, a_1, s_2]}{C[s_1, a_1]} \left(\gamma \max_{a_2} Q[s_2, a_2] \right)$$

$$s \leftarrow s'$$

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What goes wrong with this?

Evolutionary Algorithms

- Idea:
 - ▶ maintain a population of controllers
 - ▶ evaluate each controller by running it in the environment
 - ▶ at each generation, the best controllers are combined to form a new population of controllers

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- If there are n states and m actions, there are m^n policies.

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 - ▶ evaluate each controller by running it in the environment
 - ▶ at each generation, the best controllers are combined to form a new population of controllers
- If there are n states and m actions, there are m^n policies.
- Experiences are used wastefully: only used to judge the whole controller. They don't learn after every step.
- Performance is very sensitive to representation of controller.